

Past Paper Questions – Set 5

1.

$OPQR$ is a parallelogram.

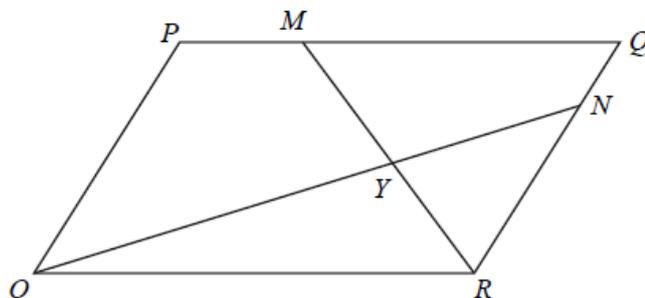


Diagram NOT accurately drawn

$\vec{OP} = 2\mathbf{a}$ and $\vec{OR} = 3\mathbf{b}$

The point M lies on PQ such that $PM = \frac{1}{4}PQ$

The point N lies on RQ such that $RN = \frac{4}{5}RQ$

(a) Find, in terms of \mathbf{a} and \mathbf{b} , giving your answers in simplest form

(i) \vec{ON}

.....
(1)

(ii) \vec{MR}

.....
(1)

MR and ON intersect at the point Y

(b) Use a vector method to find the ratio $OY : YN$.

.....
(4)

2.

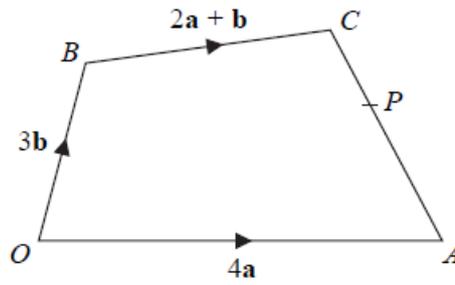


Diagram NOT
accurately drawn

The diagram shows a quadrilateral $OACB$ in which

$$\vec{OA} = 4\mathbf{a} \quad \vec{OB} = 3\mathbf{b} \quad \vec{BC} = 2\mathbf{a} + \mathbf{b}$$

- (a) Find \vec{AC} in terms of \mathbf{a} and \mathbf{b}
Give your answer in its simplest form.

$$\vec{AC} = \dots\dots\dots (2)$$

The point P lies on AC such that $AP:PC = 3:2$

The point Q is such that OPQ and BCQ are straight lines.

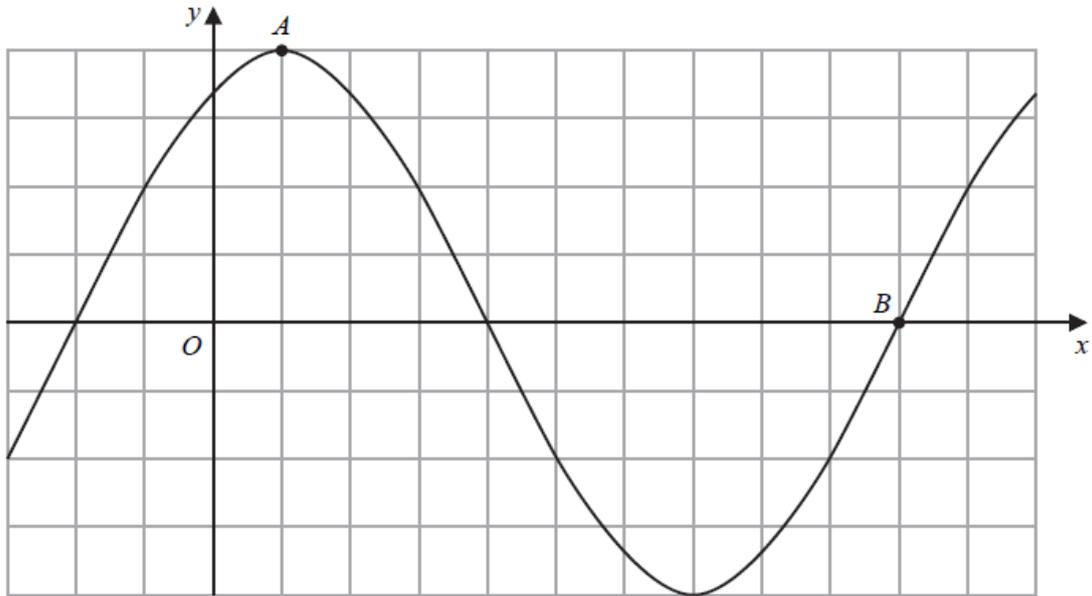
- (b) Using a vector method, find \vec{OQ} in terms of \mathbf{a} and \mathbf{b}
Give your answer in its simplest form.
Show your working clearly.

$$\vec{OQ} = \dots\dots\dots$$

(4)

3.

The diagram shows a sketch of the graph of $y = 2\sin(x + 60^\circ)$



(i) Find the coordinates of the point A

(.....,)
(1)

(ii) Find the coordinates of the point B

(.....,)
(1)

4.

- (a) Express $2x^2 - 11x + 9$ in the form $a(x - b)^2 - c$ where a , b and c are numbers to be found.

.....
(3)

The curve C has equation $y = 2(x - 3)^2 - 11(x - 3) + 9$

The point P is the minimum point on C

- (b) Find the coordinates of P

(..... ,)
(2)

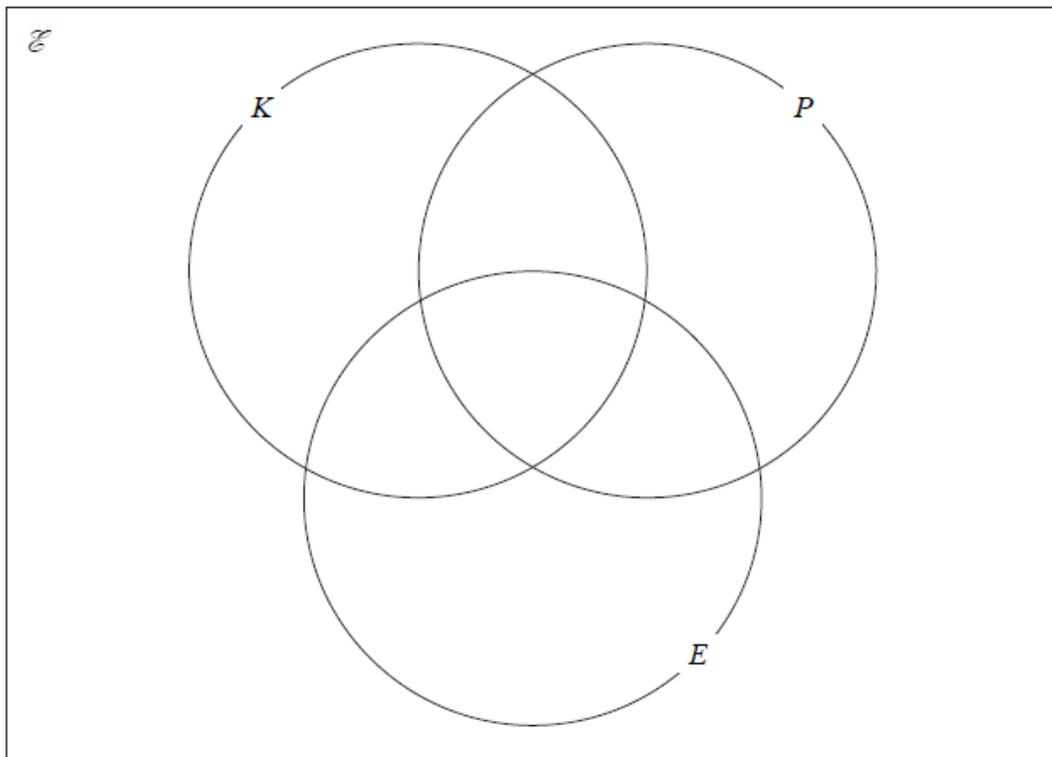
5.

60 art students were asked if they would like to attend workshops for knitting (K), for photography (P) or for embroidery (E)

Of these students

- 9 chose knitting, photography and embroidery
- 17 chose knitting and photography
- 16 chose photography and embroidery
- 20 chose knitting and embroidery
- 28 chose photography
- 39 chose embroidery
- 2 chose none of the workshops

- (a) Using this information, complete the Venn diagram to show the numbers of students in each subset.



(3)

One of the students is chosen at random.

Given that this student chose photography,

(b) find the probability that this student also chose knitting.

.....
(2)

(c) Find $n(P \cap K')$

.....
(1)

(d) Find $n([P \cup E] \cap K)$

.....
(1)

6.

There are 20 sweets in a box.

15 of the sweets are red

5 of the sweets are yellow

Fred takes at random 3 sweets from the box.

Work out the probability that Fred takes at least one sweet of each colour from the box.

(4 marks)

7.

There are 25 counters in a bag such that

6 counters are blue
 x counters are orange, where $x > 9$
the rest of the counters are pink

Maalam takes at random two of the counters from the bag.

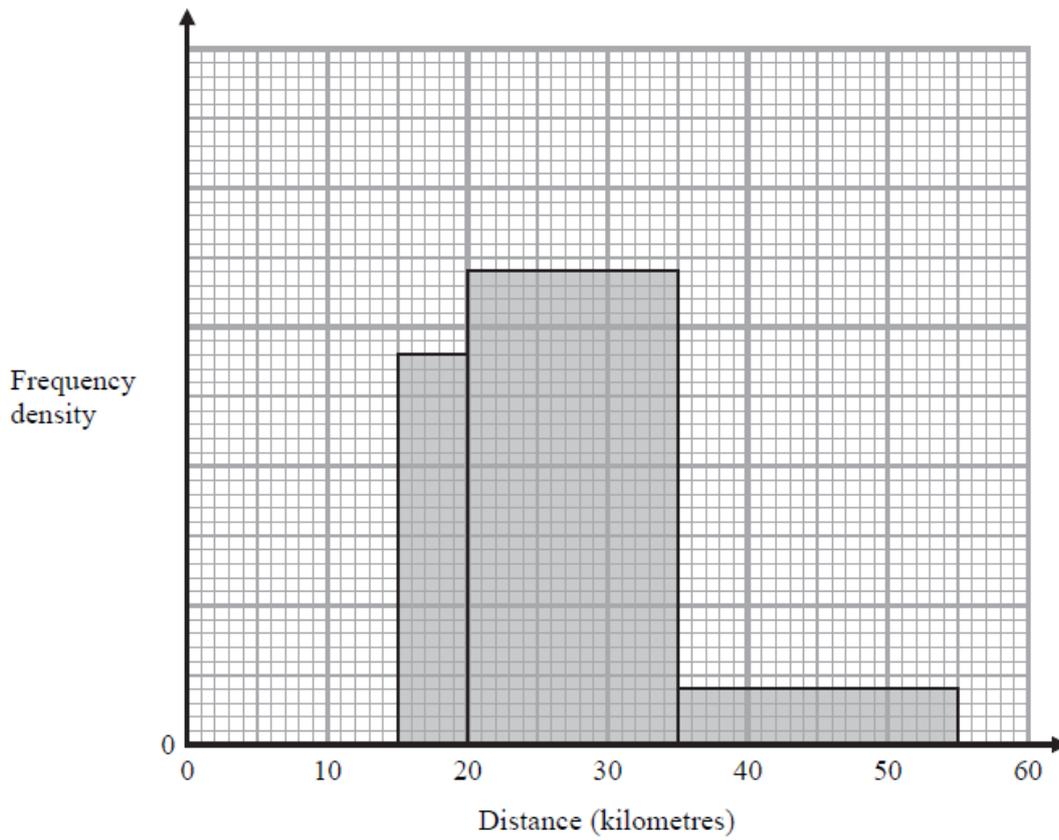
The probability that Maalam takes one orange counter and one pink counter is $\frac{22}{75}$

Calculate the probability that Maalam takes 2 pink counters from the bag.
Show clear algebraic working.

.....
(5 marks)

8.

The incomplete histogram shows some information about the distances, in kilometres, that 100 adults ran last week.



- All of the adults ran at least 5 kilometres.
- None of the adults ran more than 55 kilometres.
- 14 adults ran between 15 kilometres and 20 kilometres.

Complete the histogram.

(3 marks)