Selected Questions – Set 4 - Answers

1.

a	i	elastic potential energy and gravitational potential energy ✓	1	For elastic pe allow "pe due to tension", or "strain energy" etc
a	ii	elastic pe → kinetic energy → gravitational pe → kinetic energy → elastic pe ✓✓ [or pe→ke→pe→ke→pe is ✓ only] [or elastic pe → kinetic energy → gravitational pe is ✓ only]	2	If kinetic energy is not mentioned, no marks. Types of potential energy must be identified for full credit.
b	i	period = 0.80 s ✓ during one oscillation there are two energy transfer cycles (or elastic pe→ke→gravitational pe→ke→elastic pe in 1 cycle) or there are two potential energy maxima per complete oscillation ✓	2	Mark sequentially.
b	ii	sinusoidal curve of period 0.80 s \checkmark – cosine curve starting at $t = 0$ continuing to $t = 1.2$ s \checkmark	2	For 1 st mark allow ECF from <i>T</i> value given in 3(b)(i).
С	i	use of $T = 2\pi \sqrt{\frac{m}{k}}$ gives $0.80 = 2\pi \sqrt{\frac{0.35}{k}}$ \checkmark $\therefore k \left(= \frac{4\pi^2 \times 0.35}{0.80^2} \right) = 22 (21.6) \checkmark \text{ N m}^{-1} \checkmark$	3	Unit mark is independent: insist on N m ⁻¹ . Allow ECF from wrong T value from (b)(i): use of 0.40s gives 86.4 (N m ⁻¹).

С	ii	maximum ke = $(\frac{1}{2} m v_{\text{max}}^2) = 2.0 \times 10^{-2}$ gives		First two schemes include recognition that
		$v_{\text{max}}^2 = \frac{2.0 \times 10^{-2}}{0.5 \times 0.35} \checkmark \text{ (= 0.114 m}^2\text{s}^{-2}\text{)} \text{ and } v_{\text{max}} = 0.338 \text{ (m s}^{-1}\text{)} \checkmark$		f = 1/T i.e. $f = 1/0.80 = 1.25$ (Hz).
		$v_{\text{max}} = 2\pi f A \text{ gives } A = \frac{0.338}{2\pi \times 1.25} \checkmark$	4	Allow ECF from wrong T value from (b)(i) – 0.40s gives A = 2.15×10^{-2} m but mark to
		and $A = 4.3(0) \times 10^{-2} \text{ m} \checkmark \text{ i.e. about 40 mm}$		max 3.
		[or maximum ke = $(\frac{1}{2} m v_{\text{max}}^2)$ = $\frac{1}{2} m (2\pi f A)^2$ $\frac{1}{2} \times 0.35 \times 4\pi^2 \times 1.25^2 \times A^2 = 2.0 \times 10^{-2}$		Allow ECF from wrong k value from (c)(i) –

2.

Question	Answers	Additional Comments/Guidance	Mark
(a)(i)	$\omega \left(= \frac{v}{r} \right) = \frac{8.6}{1.5} (= 5.73 \text{ rad s}^{-1}) \checkmark$	Award full marks for any solution which arrives at the correct answer by valid physics.	3
	θ (= ωt) = 5.73 × 0.40 = 2.3 (2.29) (rad) \checkmark = $\frac{2.29}{2\pi}$ × 360 = 130 (131) (degrees) \checkmark		
	[or $s((=vt) = 8.6 \times 0.40 \ (= 3.44 \ m) \checkmark$ $\theta = \frac{3.44}{2\pi \times 1.5} \times 360 \checkmark = 130 \ (131) \ (degrees) \checkmark]$		
(a)(ii)	tension $F(=m\omega^2 r) = 0.25 \times 5.73^2 \times 1.5 \checkmark = 12(.3) \text{ (N) } \checkmark$	Estimate because rope is not horizontal.	2
	[or $F\left(=\frac{mv^2}{r}\right) = \frac{0.25 \times 8.6^2}{1.5} \checkmark = 12(.3) \text{ (N) } \checkmark \text{]}$		
(b)	maximum $\omega \left(= \sqrt{\frac{F}{mr}} \right) = \sqrt{\frac{60}{0.25 \times 1.5}} \ (= 12.6) \ (\text{rad s}^{-1}) \ \checkmark$	Allow 2 (rev s ⁻¹) for 2 nd mark. Ignore any units given in final answer.	2
	maximum $f\left(=\frac{\omega}{2\pi}\right) = \frac{12.6}{2\pi} = 2.01 \text{ (rev s}^{-1}) \checkmark$		
	[or maximum $v = \sqrt{\frac{Fr}{m}} = \sqrt{\frac{60 \times 1.5}{0.25}} $ (= 19.0) (m s ⁻¹) \checkmark		
	maximum $f\left(=\frac{v}{2\pi r}\right) = \frac{19.0}{2\pi \times 1.5} = 2.01 \text{ (rev s}^{-1}\text{) } \checkmark]$		

(C) The student's writing should be legible and the spelling, punctuation and grammar should be sufficiently accurate for the meaning to be clear.

The student's answer will be assessed holistically. The answer will be assigned to one of three levels according to the following criteria.

High Level (Good to excellent): 5 or 6 marks

The information conveyed by the answer is clearly organised, logical and coherent, using appropriate specialist vocabulary correctly. The form and style of writing is appropriate to answer the question.

The student appreciates that the velocity of the ball is not constant and that this implies that it is accelerating. There is a comprehensive and logical account of how Newton's laws apply to the ball's circular motion: how the first law indicates that an inward force must be acting, the second law shows that this force must cause an acceleration towards the centre and (if referred to) the third law shows that an equal outward force must act on the point of support at the centre. The student also understands that the rope is not horizontal and states that the weight of the ball is supported by the vertical component of the tension.

Intermediate Level (Modest to adequate): 3 or 4 marks

The information conveyed by the answer may be less well organised and not fully coherent. There is less use of specialist vocabulary, or specialist vocabulary may be used incorrectly. The form and style of writing is less appropriate.

The student appreciates that the velocity of the ball is not constant. The answer indicates how at least one of Newton's laws applies to the circular motion. The student's understanding of how the weight of the ball is supported is more superficial, the student possibly failing to appreciate that the rope would not be horizontal and omitting any reference to components of the tension.

A **high level** answer must give a reasonable explanation of the application of at least two of Newton's laws, and an appreciation of why the rope will not be horizontal.

An **intermediate level** answer must show a reasonable understanding of how at least one of Newton's laws applies to the swinging ball.

A **low level** answer must show familiarity with at least one of Newton's laws, but may not show good understanding of how it applies to this situation.

References to the effects of air resistance, and/or the need to keep supplying energy to the system would increase the value of an answer. max 6

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(c)	Low Level (Poor to limited): 1 or 2 marks		max 6
	The information conveyed by the answer is poorly organised and may not be		
	relevant or coherent. There is little correct use of specialist vocabulary. The		
	form and style of writing may be only partly appropriate.		
	The student has a much weaker knowledge of how Newton's laws apply, but		
	shows some understanding of at least one of them in this situation. The		
	answer coveys little understanding of how the ball is supported vertically.		
	The explanation expected in a competent answer should include a		
	coherent selection of the following points concerning the physical		
	 principles involved and their consequences in this case. First law: ball does not travel in a straight line, so a force must be acting on it although ball has constant speed its velocity is not constant because its direction changes constantly because its velocity is changing it is accelerating Second law: the force on the ball causes the ball to accelerate (or changes the momentum of it) in the direction of the force the acceleration (or change in momentum) is in the same direction as the force the force is centripetal: it acts towards the centre of the circle Third law: the ball must pull on the central point of support with a force that is equal and opposite to the force pulling on the ball from the centre the force acting on the point of support acts outwards Support of ball: the ball is supported because the rope is not horizontal there is equilibrium (or no resultant force) in the vertical direction the weight of the ball, mg, is supported by the vertical component of the tension, F cos θ, where θ is the angle between the rope and the vertical and F is the tension the horizontal component of the tension, F sin θ, provides the centripetal force m ω² r Credit may be given for any of these points which are described by reference to an appropriate labelled diagram. 	A reference to Newton's 3 rd law is not essential in an answer considered to be a high level response. 6 marks may be awarded when there is no reference to the 3 rd law.	

Questio	on	Answer		Guidance
(a)	(i)	$F = \frac{GM_1M_2}{(R_1 + R_2)^2}$	B1	Ignore sign
	(ii)	$F_1 = \frac{4\pi^2 M_1 R_1}{T^2}$	B1	Allow $F_1 = \left(\frac{2\pi}{T}\right)^2 M_1 R_1$
(b)		Centripetal forces on both star are same magnitude / $F_1 = F_2$ / answer to a(ii) equated to similar expression for \mathbf{S}_2	M1	Eg $\frac{4\pi^2 M_1 R_1}{T^2} = \frac{4\pi^2 M_2 R_2}{T^2}$
		Correct working starting from correct a(ii) forces	A1	
		$\frac{M_1}{M_2} = \frac{R_2}{R_1}$	AO	
(c)		$\frac{R_2}{R_1} = 3$: $R_2 = 3R_1$ and $R_1 + R_2 = 4.8 \times 10^{12}$	C1	
		$R_1 = \frac{1}{4} \times 4.8 \times 10^{12} = 1.2 \times 10^{12}$ (m) $R_2 = \frac{3}{4} \times 4.8 \times 10^{12} = 3.6 \times 10^{12}$ (m)	A1 A1	Allow 2 marks if $R_1 = 3.6 \times 10^{12}$ (m) And $R_2 = 1.2 \times 10^{12}$ (m)
(d)		$v_1 = \frac{2\pi R_1}{T} = \frac{2\pi \times 1.2 \times 10^{12}}{4 \times 3.16 \times 10^7}$ $v_1 = 6.0 \times 10^4 \text{(m s}^{-1}\text{)}$	C1	Possible ECF Mark is for substitution
		r ₁ = 0.0 × 10 (m.s.)	A1	Max 1 mark if T is not converted to seconds (leads to speed = 1.9×10^{12})

Question	Answer	Marks	Guidance
(e)	$\frac{M_1 v_1^2}{R_1} = \left(\frac{4\pi^2 R_1 M_1}{T^2}\right) = \frac{G M_1 M_2}{(R_1 + R_2)^2}$ $M_2 = \frac{\left(6.0 \times 10^4\right)^2 \times \left(4.8 \times 10^{12}\right)^2}{6.67 \times 10^{-11} \times 1.2 \times 10^{12}}$ $M_2 = 1.0 \times 10^{33} \text{(kg)}$	C1 C1 A1	Allow ECF from (c) and (d) only if method is correct Allow this C1 mark if M ₁ has been cancelled
			Special case Use of T ² ∞ R ³ will lead to 1.73 x 10 ³³ (kg) this scores 1 mark. Do not allow any ECF if this method is used.

4.

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(a)	(i)	relationship between them is $E_p = mV$ (allow $\Delta E_p = m\Delta V$) [or V is energy per unit mass (or per kg)] \checkmark	1
(a)	(ii)	value of E _p is doubled ✓	•
		value of V is unchanged ✓	2
(b)	(i)	use of $V = -\frac{GM}{r}$ gives $r_A = \frac{6.67 \times 10^{-11} \times 5.98 \times 10^{24}}{12.0 \times 10^6}$ \checkmark	2
		$= 3.3(2) \times 10^{7} (m) \checkmark$	
(b)	(ii)	since $V \propto (-)\frac{1}{r}\left(or\frac{r_A}{r_B} = \frac{V_B}{V_A} = \frac{36.0}{12.0} = 3\right)r_B = \frac{3.32 \times 10^7 m}{3} \checkmark$	1
		(which is ≈ 1.1 × 10 ⁴ km)	
(b)	(iii)	centripetal acceleration $g_{\rm B} = \frac{GM}{r_{\rm B}^2} = \frac{6.67 \times 10^{-11} \times 5.98 \times 10^{24}}{(1.11 \times 10^7)^2} \checkmark$	
		[allow use of 1.1 × 10 ⁷ m from (b) (ii)]	
		= 3.2 (m s ⁻²) ✓	2
		[alternatively, since $g_{\rm B} = (-) \frac{v_{\rm B}}{v_{\rm a}}, g_{\rm B} = \frac{36.0 \times 10^6}{1.11 \times 10^7} \checkmark$	
		= 3.2 (m s ⁻²) ✓]	
(b)	(iv)	use of $\Delta E_p = m\Delta V$ gives $\Delta E_p = 330 \times (-12.0 - (-36.0)) \times 10^6 \checkmark$	
		(which is 7.9 × 10 ⁹ J or ≈ 8 GJ)	1
(c)		g is not constant over the distance involved	
		(or g decreases as height increases or work done per metre decreases as height increases or field is radial and/or not uniform) ✓	1

	Answer	Marks	Guidance
(a)	The resultant force is zero There is no acceleration	B1 B1	Not 'in equilibrium' Not: constant velocity; since this is in the question
(b)	(moment of a force =) force × <u>perpendicular</u> distance from point / pivot	B1	Must use ticks on Scoris to show where the marks are awarded perpendicular' must be spelled correctly to gain the mark.
(c)	Forces are in the same direction / The forces are not opposite / The forces are not equal (in magnitude)	B1	
(d)	(clockwise moments =) (720 × 0.40) + (180 × 0.60) or 396 (N m)	C1	
	sum of clockwise moments = sum of anticlockwise moments		
	396 = 1.3 F	C1	Allow: 2 marks for '720 × 0.40 = 1.3 × F , F = 221 (N)' or
	F = 300 (N)	A1	180 × 0.60 = 1.3 × F, F = 83 (N)' Note: Answer is 305 (N) to 3 sf and 304.6 (N) to 4 sf
(e)	The force at X decreases	B1	
	The force at Y increases / greater clockwise moment / F_X + F_Y = 900 (N)	B1	Allow: the rider's centre of gravity / mass moves further from X