Algebra – 3B

Exercise A

Simplify the following expressions where possible.

$$1 \ 3a + 5a$$

$$2 6x - 2x$$

$$3 4a + 3b$$

$$4 6c - 4d$$

$$5 3d + d$$

6
$$3x + 2$$

$$7 \quad 7y + 2y$$

$$8 \quad 5h - 3h$$

$$9 \ 8w - 5w$$

$$10 6y - 5y$$

11
$$7x + y$$

$$12 8m + m$$

$$14 + 6m + 5n$$

$$15 \ 4x + 6$$

$$16 \ 5b + 8b$$

$$17 20t - 8t$$

18
$$7p - 6p$$

19
$$10n + 15n$$

$$21 8x + 2$$

$$22 \quad 14h + 16h$$

$$23 9 - 7x$$

$$25 7a + 6$$

$$26 \ 5c + c$$

$$28 \quad 12y - y$$

Exercise B

Simplify the following expressions as far as possible by collecting like terms.

$$1 \quad 3a + 5b + 3a + 2b$$

$$2 2x + 4y + 7x + 3y$$

$$3 8x + 4y - 5x - 2y$$

$$4 7m + 5n - 4m + 3n$$

$$5 6a + 5 + a + 4$$

$$6 8a + 3b - 6a + 4b$$

7
$$5x + 9 - 2x - 7$$

$$8 7p + 9q + 2p - 4q$$

9
$$7x + 8 + x - 6$$

$$10 \quad a + 14b + 5a - 4b$$

11
$$6m + 8 + 6m - 7$$

12
$$3h + 20 - h + 5$$

13
$$5m + 2n + 4n + 7m$$

14
$$8p + 6q - 3q - 2p$$

17 8a + 3b - 4a + 4c

15
$$6x + 10 - 6 + 3x$$

16
$$7x + 3y + x + 6$$

$$20 4y + 8 - 5 - 3y$$

19
$$8 + 4a + 7 - 2a$$

22 $5p + 6q + 4p - 4q$

23
$$7m + 9n - 7n + 4$$

$$24 + 6x + 8 - x + 9x$$

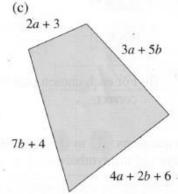
25 Write down an expression for the perimeter of each shape below. Collect like terms where possible.

(a) 2x+6 4x

4x + 3

(b) 3m + n 5n 4n + m 5m





Which two expressions below are *equivalent* (this means they give the same answer when the like terms are collected).

3m + n

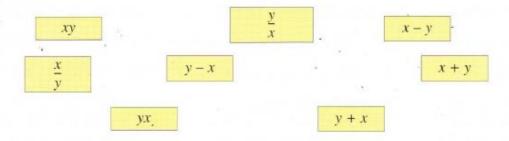
(a)
$$5x + 3 - 2x + 6y + x$$

(b)
$$3y + 4x + 3y + 6 - 2$$

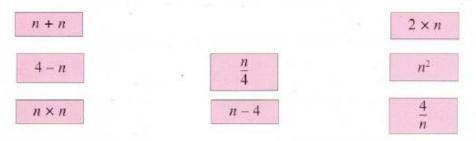
(c)
$$7 + 4y + 4x + 2y - 3$$

Exercise C

1 (a) Write down any pairs of expressions from below that are equal to each other.



- (b) For each chosen pair from part (a), write down a pair of values for x and y which show that you are correct.
- 2 (a) Write down any pairs of expressions from below that are equal to each other.



(b) For each chosen pair from part (a), write down a value for n which shows that you are correct.

In questions 3 to 14 write down each statement and say whether it is 'true' or 'false' for all values of the symbols used.

If you are not sure, try different values for the letters

$$3 \quad x + x + x = 3x$$

$$4 \quad xw = wx$$

5
$$m \times m = 2m$$

$$6 \quad m+n=n+m$$

$$7 \quad 5y - y = 5$$

$$8 \quad a \times 5 = 5a$$

$$9 \quad \frac{x}{2} = \frac{2}{x}$$

$$10 \quad a \times a \times a = 3a$$

$$11 \quad a^2 = 2a$$

12
$$a \div 3 = 3 \div a$$

13
$$\frac{1}{2}$$
 of $b = \frac{b}{2}$

$$14 \quad 3n^2 = (3n)^2$$

15 Simplify the following expressions.

(a)
$$\frac{m}{m}$$

(b)
$$\frac{4a}{4}$$

(c)
$$\frac{n^2}{n}$$

(d)
$$\frac{6x}{x^i}$$

Exercise D

Simplify

 $1 \quad 4a \times 2b$

2 5c × 3d

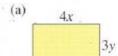
 $3 \quad 6m \times 7n$

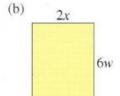
 $3p \times 8q$

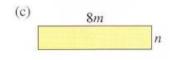
 $9b \times 2a$

6 $2m \times n \times 5p$

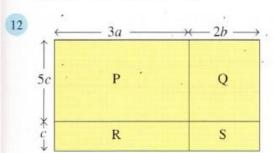
- 7 $7a \times 3b \times 2c$
- $4q \times 6r \times p$
- $5a \times 3 \times 2b$
- 10 Use algebra to write down an expression for the area of each rectangle below.







- 11 Simplify by collecting like terms
 - (a) pq + qp
 - (c) 5m + nm + 3mn 2m
 - (e) x + y + xy + 3yx x + 3xy
 - (g) 2a + 3ba a + 5ab 2ba
- (b) 3xy + 4mn 2mn + 4yx
- (d) 4ab + 3a 2ba a + 3ab
- (f) 6cd + 4dc + ab 2c + 3cd + ba
- (h) 3q + 4pq 2q + 3qp + 4



- Use algebra to write down an expression for the area of each of the following:
- (a) P
- (b) O
- (c) P + R
- (d) S
- (e) Q + S (f) P + Q + R + S

- 13 What must be added to 6ba to give 8ab?
- What must be added to 3x + 7yx to give 5x + 8xy?
- 15 Neil multiplies two algebraic terms together and gets the answer 12ab. Write down all the different pairs of terms that Neil may have used (numbers used must be whole numbers).

Exercise E

In Questions 1 to 20 collect like terms together.

1.
$$2x + 3 + 3x + 5$$

3.
$$5x - 3 + 2x + 7$$

5.
$$4x - 3 + 2x + 10 + x$$

7.
$$7x - 9 + 2x + 3 + 3x$$

9.
$$4x - 6 - 2x + 1$$

11.
$$4a + 6b + 3 + 9a - 3b - 4$$

13.
$$6p - 4 + 5q - 3p - 4 - 7q$$

15.
$$a-2b-7+a+2b+8$$

17.
$$6x - 5y + 3z - x + y + z$$

19.
$$12a - 3 + 2b - 6 - 8a + 3b$$

2.
$$4x + 8 + 5x - 3$$

4.
$$6x + 1 + x + 3$$

6.
$$5x + 8 + x + 4 + 2x$$

8.
$$5x + 7 - 3x - 2$$

10.
$$10x + 5 - 9x - 10 + x$$

12.
$$8m - 3n + 1 + 6n + 2m + 7$$

14.
$$12s - 3t + 2 - 10s - 4t + 12$$

16.
$$3x + 2y + 5z - 2x - y + 2z$$

18.
$$2k - 3m + n + 3k - m - n$$

20.
$$3a + x + e - 2a - 5x - 6e$$

21. Simplify where possible.

(a)
$$x^2 - 3x + 1 + 2x^2 + 3x$$

(c) $x^3 - 7x + 4x^2$

(b)
$$5a + ab - 3a + 4ab$$

(c)
$$x^3 - 7x + 4x^2$$

(d)
$$ab + 3a^2 - 7a - ab + a^2$$

22. Which of these expressions is equivalent to x - 2?

A
$$x^2 - 7x - 1 - x^2 + 8x + 3$$

C
$$5+7x-x-4-6x+x^2$$

B
$$x^2 + 7x + 2x - 8x - x^2 - 2$$

D
$$5x - 7 + 4 - x + 1 - 3x$$

Collect like terms together.

23.
$$x^2 + 5x + 2 - 2x + 1$$

25.
$$x^2 + 5x + x^2 + x - 7$$

27.
$$3x^2 + 4x + 6 - x^2 - 3x - 3$$

29.
$$2x^2 - 2x + 3 - x^2 - 2x - 5$$

31.
$$3v^2 - 6x + v^2 + x^2 + 7x + 4x$$

23.
$$x^2 + 5x + 2 - 2x + 1$$

25. $x^2 + 5x + x^2 + x - 7$
27. $3x^2 + 4x + 6 - x^2 - 3x - 3$
29. $2x^2 - 2x + 3 - x^2 - 2x - 5$
31. $3y^2 - 6x + y^2 + x^2 + 7x + 4x^2$
33. $5 + 2y + 3y^2 - 8y - 6 + 2y^2 + 3$
35. $3c^2 - d^2 + 2cd - 3c^2 - d^2$
37. $x^3 + 2x^2 - x + 3x^2 + x^3 + x$

35.
$$3c^2 - d^2 + 2cd - 3c^2 - d^2$$

37.
$$r^3 + 2r^2 - r + 3r^2 + r^3 + r$$

39.
$$xy + ab - cd + 2xy - ab + dc$$

24.
$$x^2 + 2x + 2x^2 + 4x + 5$$

26.
$$2x^2 - 3x + 8 + x^2 + 4x + 4$$

28. $5x^2 - 3x + 2 - 3x^2 + 2x - 2$
30. $6x^2 - 7x + 8 - 3x^2 + 5x - 10$

28.
$$5x^2 - 3x + 2 - 3x^2 + 2x - 2$$

30.
$$6x^2 - 7x + 8 - 3x^2 + 5x - 10$$

32.
$$8-5x-2x^2+4+6x+2x$$

34.
$$ab + a^2 - 3b + 2ab - a^2$$

36.
$$ab + 2a^2 + 3ab - 4a^2 + 2a$$

32.
$$8 - 5x - 2x^2 + 4 + 6x + 2x^2$$

34. $ab + a^2 - 3b + 2ab - a^2$
36. $ab + 2a^2 + 3ab - 4a^2 + 2a$
38. $5 - x^2 - 2x^3 + 6 + 2x^2 + 3x^3$
40. $pq - 3qp + p^2 + 2qp - q^2$

40.
$$pq - 3qp + p^2 + 2qp - q^2$$