

Short Assessment 2

Time Allowed: 15 minutes

Total Marks: 15

1. Find the discriminant of the following quadratic expressions:

(a) $2x^2 + 3x - 6$

$$\begin{aligned}\Delta &= b^2 - 4ac \\ &= 3^2 - 4(2)(-6) \\ &= \underline{\underline{57}}\end{aligned}$$

(b) $3x^2 - 5x + 2$

$$\begin{aligned}\Delta &= b^2 - 4ac \\ &= (-5)^2 - 4(3)(2) \\ &= \underline{\underline{1}}\end{aligned}$$

(2 marks)

2. Use the discriminant to determine the number of real roots of each of the following quadratic equations:

(a) $x^2 + 5x - 2 = 0$

$$\begin{aligned}\Delta &= b^2 - 4ac \\ &= 5^2 - 4(1)(-2) = 33 > 0\end{aligned}$$

Since $\Delta > 0$, there are two distinct real roots.

(b) $2x^2 - 3x + 6 = 0$

$$\begin{aligned}\Delta &= (-3)^2 - 4(2)(6) \\ &= -39 < 0\end{aligned}$$

Since $\Delta < 0$, there are no real roots to this equation.

(4 marks)

3. (a) Find the discriminant of $2x^2 - 5x + k$ in terms of k .

$$\begin{aligned}\Delta &= b^2 - 4ac \\ &= (-5)^2 - 4(2)k \\ &= \underline{\underline{25 - 8k}}\end{aligned}$$

(2 marks)

- (b) Given that the quadratic equation $2x^2 - 5x + k = 0$ has two distinct real roots, find the set of possible values of k .

Since the equation has two distinct real roots,

$$\Delta > 0$$

$$25 - 8k > 0$$

$$25 > 8k$$

$$\frac{25}{8} > k$$

$$\therefore k < \underline{\underline{\frac{25}{8}}}$$

(3 marks)

4. The quadratic equation $px^2 + 7x + p = 0$ has repeated real roots.

Find the possible values of the constant p .

Since this has repeated real roots,

$$b^2 - 4ac = 0$$

$$7^2 - 4(p)(p) = 0$$

$$49 = 4p^2$$

$$p^2 = \frac{49}{4}$$

$$p = \pm \frac{7}{2} //$$

(4 marks)

- End of Test -