

Exercise A

- 1 0K is the lowest temperature as at this temperature the internal energy of a substance is at its minimum value. The kinetic energy of all the atoms or molecules is zero - they have stopped moving. [1]
- 2 Increases the internal energy of the substance as the electrostatic potential increases when a substance changes phase (from solid to liquid, or from liquid to gas). [1]
- 3 Increase the temperature of the substance. [1]
Change the phase of the substance from solid to liquid, or from liquid to gas. [1]
- 4 The average kinetic energy of the atoms or molecules in 1.0kg of water at 0°C is the same as the average kinetic energy of the atoms or molecules in 1.0kg of ice at 0°C.
However, the atoms or molecules in 1.0kg of water have a higher electrostatic potential energy. [1]
As the internal energy is the sum of the kinetic and potential energies of the atoms or molecules within the substance. The water has a higher internal energy. [1]
- 5 When the water vapour condenses there is a decrease in the electrostatic potential energy of the particles in the water. [1]
This energy is transferred from the water to the window. [1]

Exercise B

- 1 a Use of $E = mc\Delta\theta$ [1]
Water: $E = 1.0 \times 4200 \times 20 = 84000\text{J}$ [1]
b Aluminium: $E = 0.600 \times 904 \times 20 = 10800\text{J}$ [1]
c Lead: $E = 4.2 \times 10^{-6} \times 129 \times 20 = 10.8\text{mJ}$ [1]
- 2 Appropriate diagram [2]
Measurements: Current [1]
Potential difference [1]
Initial temperature [1]
Final temperature [1]
Time [1]

- 3 Change in GPE is converted into thermal energy. [1]
 Loss in GPE = $mg\Delta h = 1.0 \times 9.81 \times 450 = 4400 \text{ J}$ [1]
 $E = mc\Delta\theta$ Therefore $\Delta\theta = \frac{E}{mc} = \frac{4400}{1.0 \times 4200} = 1.0^\circ\text{C}$ [1]
- 4 $c = \frac{IVt}{m\Delta\theta}$ [1]
 $c = \frac{2.0 \times 12 \times (5.0 \times 60)}{0.500 \times 32}$ [1]
 $c = 450 \text{ J kg}^{-1} \text{ K}^{-1}$ this corresponds to iron in Table 1 [1]
- 5 From $E = mc\Delta\theta$: $P = mc \frac{\Delta\theta}{\Delta t}$ [1]
 From the graph $\frac{\Delta\theta}{\Delta t} = \text{gradient}$ [1]
 Gradient = $0.75^\circ\text{C s}^{-1} \pm 0.04^\circ\text{C s}^{-1}$ [1]
 $P = mc \frac{\Delta\theta}{\Delta t} = mc \text{ gradient}$ and therefore
 $c = \frac{P}{m \times \text{gradient}}$ [1]
 $c = \frac{60}{0.030 \times 0.75} = 270 \text{ J kg}^{-1} \text{ K}^{-1} \pm 200 \text{ J kg}^{-1} \text{ K}^{-1}$ [1]
- 6 Drop in kinetic energy of car
 $= \frac{1}{2}mv^2 = \frac{1}{2} \times 1500 \times 20^2 = 300 \text{ kJ}$ [1]
 As there are two discs the energy dissipated by
 each disc = 150 kJ [1]
 $E = mc\Delta\theta$ therefore $\Delta\theta = \frac{E}{mc} = \frac{150000}{8.0 \times 500} = 38^\circ\text{C}$ [1]

Exercise C

- 1 $E = mL_f$ [1]
 $E = 2.5 \times 88000 = 220 \text{ kJ}$ [1]
- 2 There is a greater change in internal energy changing
 phase from liquid to gas than from solid to liquid. [1]
- 3 $E = mL_f$ [1]
 $E = 0.050 \times 398000 = 20 \text{ kJ}$ [1]
- 4 Energy transferred to the water = $Pt = 24 \times (60 \times 20)$
 $= 28800 \text{ J}$ [1]
 $E = mL_v$, $m = \frac{E}{L_v}$ [1]
 $m = \frac{28800}{2.26 \times 10^6} = 0.013 \text{ kg}$ [1]
- 5 a $\frac{E}{\Delta t} = mc \frac{\Delta\theta}{\Delta t}$ [1]
 $\frac{E}{\Delta t} = 0.060 \times 904 \times \frac{640}{16}$ [1]
 $\frac{E}{\Delta t} = 2200 \text{ W}$ [1]
- b $E = mL_f$ [1]
 $E = 0.060 \times 398000 = 24000 \text{ J}$ [1]

$$6 \quad \text{Kinetic energy of bullet} = \frac{1}{2}mv^2 = \frac{1}{2} \times 0.008 \times 400^2 = 640 \text{ J} \quad [1]$$

Energy required to heat the bullet to its melting point (327 °C):

$$E = mc\Delta\theta = 0.008 \times 129 \times (327 - 20) = 296 \text{ J} \quad [1]$$

Exercise D

$$1 \quad N = n \times N_A = 3.0 \times 6.02 \times 10^{23} \quad [1]$$

$$N = 1.8 \times 10^{24} \text{ atoms or molecules} \quad [1]$$

2 The number of atoms in 1 mol of silicon is the same as the number of atoms in 1 mol of aluminium. [1]

However, the atoms have a different mass (silicon atoms have a greater mass than aluminium atoms). [1]

3 Initial momentum = mu and final momentum = $-mu$ [1]

Therefore change in momentum, $\Delta p = 2mu$ [1]

$$4 \quad \text{a} \quad N = n \times N_A \text{ therefore } n = \frac{N}{N_A}$$

$$n = \frac{N}{N_A} = \frac{2.0 \times 10^{24}}{6.02 \times 10^{23}} = 3.3 \text{ mol} \quad [1]$$

$$\text{b} \quad n = \frac{N}{N_A} = \frac{1.5 \times 10^{17}}{6.02 \times 10^{23}} = 2.5 \times 10^{-7} \text{ mol} \quad [1]$$

$$\text{c} \quad n = \frac{N}{N_A} = \frac{2.0 \times 10^{24}}{6.02 \times 10^{23}} = 3.3 \text{ mol} \quad [1]$$

$$5 \quad \text{a} \quad m = n \times M = \frac{N}{N_A} \times M \text{ therefore } N = \frac{m \times N_A}{M} \quad [1]$$

$$= \frac{1.0 \times 6.02 \times 10^{23}}{64 \times 10^{-3}} = 9.4 \times 10^{24} \quad [1]$$

$$\text{b} \quad m = n \times M = \frac{N}{N_A} \times M$$

Find m when $N = 1$ [1]

$$M = \frac{1}{6.02 \times 10^{23}} \times 235 \times 10^{-3} = 3.9 \times 10^{-25} \text{ kg}$$

6 Mass of lead, density = $\frac{\text{mass}}{\text{volume}}$ therefore

$$\text{mass} = \text{density} \times \text{volume} \quad [1]$$

$$\text{mass} = 11340 \times 0.20 = 2300 \text{ kg} \quad [1]$$

$$\text{Number of atoms} = \frac{2300}{3.46 \times 10^{-25}} = 6.6 \times 10^{27} \text{ atoms} \quad [1]$$

$$n = \frac{N}{N_A} = \frac{6.6 \times 10^{27}}{6.02 \times 10^{23}} = 11 \times 10^3 \text{ mol} \quad [1]$$

Exercise E

- 1 $pV = nRT$ therefore $p = \frac{nRT}{V}$ [1]
 $p = \frac{60 \times 8.31 \times 250}{60000} = 2.1 \text{ Pa}$ [1]
- 2 a $p \propto \frac{1}{V}$ therefore if V is doubled, p halves. [1]
 b $p \propto \frac{1}{V}$ therefore if V reduces by a factor of 3,
 p increases by a factor of 3. [1]
- 3 $\frac{p}{T} = \text{constant}$ [1]
 Initially: $\frac{300000}{293} = 1020 \text{ Pa K}^{-1}$ [1]
 $p = \text{constant} \times T$
 After the change $p = 1020 \times 393 = 401000 \text{ Pa}$ [1]
 Therefore the change = 101 000 Pa [1]
- 4 Graph of p against $\frac{1}{V}$ with axis labelled (including units) [1]
 Points plotted correctly [1]
 Line of best fit drawn [1]
 Determination of gradient = 48 000 +/- 2000 [1]
 Gradient = nRT therefore $n = \frac{\text{gradient}}{RT}$
 $n = \frac{48000}{8.31 \times 293} = 20 \text{ mol}$ [1]
- 5 $pV = nRT$ therefore $V = \frac{nRT}{p}$ [1]
 $V = \frac{1 \times 8.31 \times 273}{100000}$ [1]
 $V = 0.023 \text{ m}^3$ [1]
- 6 $pV = nRT$ therefore $n = \frac{pV}{RT}$ [1]
 $n = \frac{50000 \times 0.25}{8.31 \times 288}$ [1]
 $n = 5.2 \text{ mol}$ [1]
 $N = n \times N_A = 5.2 \times 6.02 \times 10^{23}$
 $= 3.1 \times 10^{24}$ particles (atoms or molecules) [1]
- 7 $pV = nRT$ therefore $n = \frac{RT}{pV}$ [1]
 Temperature of air inside the lungs - 300 K
 Volume of the lungs - 5800 ml \rightarrow 0.0058 m³ [1]
 Pressure in the lungs - atmospheric pressure
 $= 100000 \text{ Pa}$
 $n = \frac{8.31 \times 300}{100000 \times 0.0058}$ [1] - mark awarded for using
 your estimates
 $n = 4.3 \text{ mol}$ [1]

Exercise F

$$1 \quad \text{Mean speed} = \frac{100 + 200 + 150 + 50}{4} = 125 \text{ m s}^{-1} \quad [1]$$

$$\text{Mean square speed} = \frac{100^2 + 200^2 + 150^2 + 50^2}{4} \\ = 19000 \text{ m}^2 \text{ s}^{-2} \quad [1]$$

$$\text{Root mean square speed} = \sqrt{19000} = 140 \text{ m s}^{-1} \quad [1]$$

2 Particles gain kinetic energy as the temperature increases [1]

Therefore the speeds of the particles increases [1]

$$3 \quad pV = \frac{1}{3} Nmc^2 \quad \text{therefore} \quad V = \frac{\frac{1}{3} Nmc^2}{p} \quad [1]$$

$$V = \frac{\frac{1}{3} \times 4.0 \times 10^{25} \times 4.7 \times 10^{-26} \times 450^2}{800000} \quad [1]$$

$$V = 0.16 \text{ m}^3 \quad [1]$$

$$4 \quad pV = \frac{1}{3} Nmc^2 \quad \text{therefore} \quad p = \frac{\frac{1}{3} Nmc^2}{V} \quad [1]$$

$$p = \frac{\frac{1}{3} \times 4.0 \times 10^{25} \times 4.7 \times 10^{-26} \times 600^2}{0.16} \quad [1]$$

$$p = 1.4 \text{ MPa} \quad [1]$$

$$5 \quad \text{a} \quad N = n \times N_A = 2.0 \times 6.02 \times 10^{23} \\ = 1.2 \times 10^{24} \text{ molecules} \quad [1]$$

$$\text{b} \quad \text{mass of molecule} = \frac{M}{N} = \frac{0.032}{1.2 \times 10^{24}} \\ = 2.7 \times 10^{-26} \text{ kg} \quad [1]$$

$$\text{c} \quad pV = \frac{1}{3} Nmc^2 \quad \text{therefore} \quad c^2 = \frac{pV}{\frac{1}{3} Nm} \quad [1]$$

$$c^2 = \frac{140000 \times 0.020}{\frac{1}{3} \times 1.2 \times 10^{24} \times 2.7 \times 10^{-26}} \quad [1]$$

$$c^2 = 260000 \text{ m}^2 \text{ s}^{-2} \quad [1]$$

$$c_{\text{rms}} = \sqrt{260000} = 510 \text{ m s}^{-1} \quad [1]$$