Answers - Differentiation (Year 12)

iii 6.1

Exercise A

2.

- a i 7 iv 6.01
- ii 6.5
- $\mathbf{v} = h + 6$
- **b** 6

3.

- ii 8.5
- iii 8.1

- a i 9 iv 8.01
- v 8+h
- **b** 8

Exercise B

- $7 -3x^{-4}$

- 10 $-5x^{-6}$

- 13 $-2x^{-3}$.
- 14 1
- 15 3x2

- 16 9x8
- 17 5x4
- 18 3x2

Exercise C

- $\mathbf{a} 4x 6$
- **b** x + 12 **c** 8x

- **d** 16x + 7
- **e** 4 10x
- a 12
- **b** 6
 - c 7

- **d** $2\frac{1}{2}$
- **e** −2
- f 4

- 4, 0
 - 4 (-1, -8)
- 1, -1 6 6, -4

Exercise D

$$b - x^{-3}$$

3 a
$$(2\frac{1}{2}, -6\frac{1}{4})$$

1 **a**
$$4x^3 - x^{-2}$$
 b $-x^{-3}$ **c** $-x^{-\frac{2}{3}}$
2 **a** 0 **b** $11\frac{1}{2}$
3 **a** $(2\frac{1}{2}, -6\frac{1}{4})$ **b** $(4, -4)$ and $(2, 0)$
c $(16, -31)$ **d** $(\frac{1}{2}, 4)$ $(-\frac{1}{2}, -4)$

d
$$(\frac{1}{2}, 4)$$
 $(-\frac{1}{2}, -4)$

Exercise E

d
$$\frac{4}{3}x^3 - 2x^2$$

1 **a**
$$x^{-\frac{1}{2}}$$
 b $-6x^{-3}$ **c** $-x^{-4}$ **d** $\frac{4}{3}x^3 - 2x^2$ **e** $-6x^{-4} + \frac{1}{2}x^{-\frac{1}{2}}$

f
$$\frac{1}{3}x^{-\frac{2}{3}} - \frac{1}{2}x^{-2}$$
 g $-3x^{-2}$ **h** $3 + 6x^{-2}$

$$g -3x^{-2}$$

h
$$3 + 6x^{-2}$$

i
$$5x^{\frac{3}{2}} + \frac{3}{2}x^{-\frac{1}{2}}$$
 j $3x^2 - 2x + 2$ k $12x^3 + 18x^2$

$$3x^2 - 2x + 2$$

$$k 12x^3 + 18x^2$$

1
$$24x - 8 + 2x^{-2}$$

2 **a** 1 **b** $\frac{2}{9}$ **c** -4 **d** 4

1
$$24x - 8 + 2x$$

Exercise F

1
$$24x + 3, 24$$

2
$$15-3x^{-2}$$
, $6x^{-3}$

3
$$\frac{9}{2}x^{-\frac{1}{2}} + 6x^{-3}, -\frac{9}{4}x^{-\frac{3}{2}} - 18x^{-4}$$

4
$$30x + 2,30$$

5
$$-3x^{-2} - 16x^{-3}$$
, $6x^{-3} + 48x^{-4}$

Exercise G

$$2 2\pi$$

1
$$2t-3$$

3 $-12t^{-2}$
5 $1-5r^{-2}$

$$6 -12 + 8t$$

7
$$10-2x$$

Exercise H

1 **a**
$$y + 3x - 6 = 0$$
 b $4y - 3x - 4 = 0$
c $3y - 2x - 18 = 0$ **d** $y = x$
e $y = 12x + 14$ **f** $y = 16x - 22$

$$3y - 2x - 18 = 0$$
 d $y = 0$

e
$$y = 12x + 14$$
 f $y = 16x - 22$

2 a
$$7y + x - 48 = 0$$
 b $17y + 2x - 212 = 0$

3
$$(1^2_9, 1^8_9)$$

4
$$y = -x$$
, $4y + x - 9 = 0$

5
$$y = -8x + 10$$
, $8y - x - 145 = 0$